

Name: Answer Key

Date: _____

Lesson #113- Solving for the Measure of an Angle Algebraically

Essential Question: How can we use the properties of angles to solve for the measure of a missing angle algebraically?

Do Now: Solve the following equations for x !

1. $3x + 6 = 48$

$$\begin{array}{r} 3x + 6 = 48 \\ -6 \quad -6 \\ \hline 3x = 42 \\ \div 3 \quad \div 3 \\ \hline x = 14 \end{array}$$

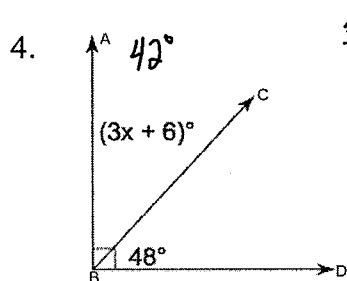
2. $5x + 3x = 8$

$$\begin{array}{r} 5x + 3x = 8 \\ 8x = 8 \\ \div 8 \quad \div 8 \\ \hline x = 1 \end{array}$$

3. $5x + 12 = 8x - 3$

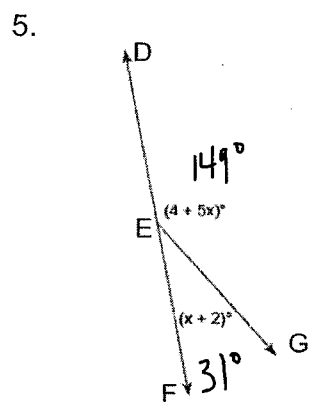
$$\begin{array}{r} 5x + 12 = 8x - 3 \\ -5x \quad -5x \\ \hline 12 = 3x - 3 \\ \div 3 \quad \div 3 \\ \hline 5 = x \end{array}$$

Directions: Find the value of x algebraically. Then, identify the measure of the missing angle(s).



$$\begin{array}{r} 3x + 6 + 42 = 90 \\ 3x + 48 = 90 \\ -48 \quad -48 \\ \hline 3x = 42 \\ \div 3 \quad \div 3 \\ \hline x = 14 \end{array}$$

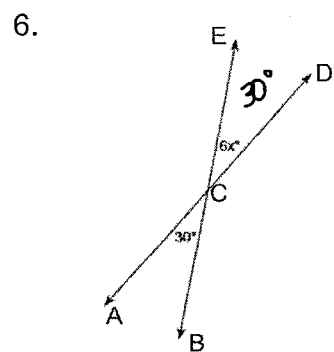
$$\begin{array}{l} m\angle ABC = 3x + 6 \\ m\angle ABC = 3(14) + 6 \\ m\angle ABC = 42 + 6 \\ m\angle ABC = 48^\circ \end{array}$$



$$\begin{array}{r} 4 + 5x + x + 2 = 180 \\ 6 + 6x = 180 \\ -6 \quad -6 \\ \hline 6x = 174 \\ \div 6 \quad \div 6 \\ \hline x = 29 \end{array}$$

$$\begin{array}{l} m\angle DEG = 4 + 5x \\ m\angle DEG = 4 + 5(29) \\ m\angle DEG = 149^\circ \end{array}$$

$$\begin{array}{l} m\angle FEG = x + 2 \\ m\angle FEG = 29 + 2 \\ m\angle FEG = 31^\circ \end{array}$$



$$\begin{array}{r} 30 = 6x \\ \div 6 \quad \div 6 \\ \hline 5 = x \end{array}$$

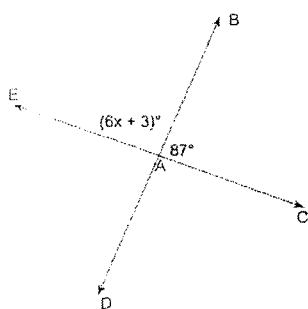
$$\begin{array}{l} m\angle ECD = 6x \\ m\angle ECD = 6(5) \\ m\angle ECD = 30^\circ \end{array}$$

Steps for solving for the value of a missing angle algebraically:

1. Identify the angle relation
2. Set up the appropriate equation
3. Solve for x.
4. Substitute the identified value of x in for the angle value and solve

Directions: Using the properties of angles, solve for the value of x. Then, identify the measure of the missing angle(s).

7.



$$6x + 3 + 87 = 180$$

$$6x + 90 = 180$$

$$\begin{array}{r} -90 \\ -90 \end{array}$$

$$\frac{6x}{6} = \frac{90}{6}$$

$$x = 15$$

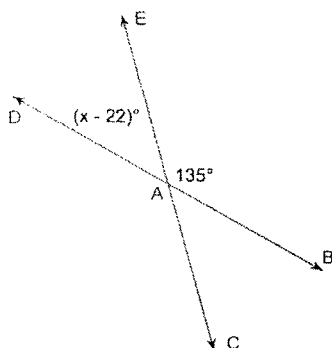
$$m\angle EAB = 6x + 3$$

$$m\angle EAB = 6(15) + 3$$

$$m\angle EAB = 93^\circ$$

Value of x = 15 $m\angle EAB =$ 93°

8.



$$x - 22 + 135 = 180$$

$$x + 113 = 180$$

$$\begin{array}{r} -113 \\ -113 \end{array}$$

$$x = 67$$

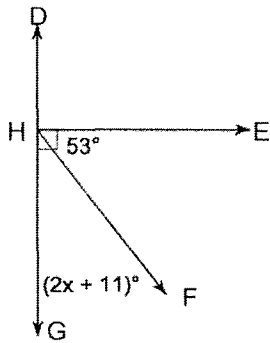
$$m\angle DAE = x - 22$$

$$m\angle DAE = 67 - 22$$

$$m\angle DAE = 45^\circ$$

Value of x = 67 $m\angle DAE =$ 45°

9.



$$2x + 11 + 53 = 90$$

$$2x + 64 = 90$$

$$\underline{-64 \quad -64}$$

$$\frac{2x}{2} = \frac{26}{2}$$

$$x = 13$$

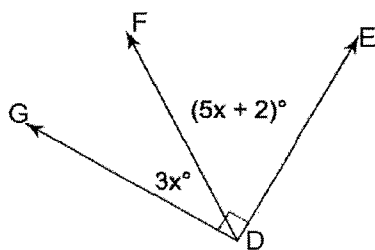
$$m\angle FGH = 2x + 11$$

$$m\angle FGH = 2(13) + 11$$

$$m\angle FGH = 37^\circ$$

Value of $x =$ 13 $m\angle FGH =$ 37^\circ

10.



$$3x + 5x + 2 = 90$$

$$8x + 2 = 90$$

$$\underline{-2 \quad -2}$$

$$\frac{8x}{8} = \frac{88}{8}$$

$$x = 11$$

$$m\angle EDF = 5x + 2$$

$$m\angle EDF = 5(11) + 2$$

$$m\angle EDF = 57^\circ$$

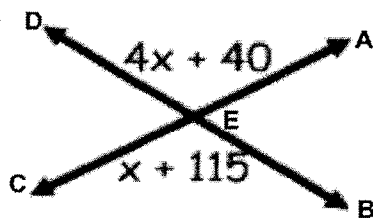
$$m\angle FDG = 3x$$

$$m\angle FDG = 3(11)$$

$$m\angle FDG = 33^\circ$$

Value of $x =$ 11 $m\angle EDF =$ 57^\circ $m\angle FDG =$ 33^\circ

11.



$$4x + 40 = x + 115$$

$$\underline{-x \quad -40 \quad -x \quad -40}$$

$$\frac{3x}{3} = \frac{75}{3}$$

$$x = 25$$

$$m\angle DEA = 4x + 40$$

$$m\angle DEA = 4(25) + 40$$

$$m\angle DEA = 140^\circ$$

$$m\angle CEB = x + 115$$

$$m\angle CEB = 25 + 115$$

$$m\angle CEB = 140^\circ$$

Value of $x =$ 25 $m\angle DEA =$ 140^\circ $m\angle CEB =$ 140^\circ

